

Holiday effects in the South African futures market

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International and local research in share markets offered evidence of a holiday effect. Pre-holiday mean returns are significantly higher than on other trading days. The holiday effect cannot be separated from the weekend effect, as holidays which fall on Fridays and Mondays also influence the weekend analysis. Both these effects exist in their own right. Research on international futures markets supports the existence of a holiday effect. The present study investigates the holiday effect on daily returns of the All Gold Near Futures contract, the All Industrial Near Futures contract and the All Share Near Futures contract in the South African futures market. A distinction is made between pre-holidays, post-holidays and non-holidays. None of the near futures contracts exhibit a significant holiday effect, although signs of a holiday effect are present. It is further shown that the month-end effect is not strongly influenced by the holiday effect. It is also concluded that the pre-holiday effects are not large enough to be exploited on an on-going basis in the South African futures market.

Introduction

Since the turn of the century various studies have focussed on determining seasonal anomalies in financial markets. The main focus had been on share markets and long-term bond markets. Most of the research was initiated in the United States and further research followed in other international markets. Empirical evidence has been provided by various researchers in support of seasonal anomalies, such as the day-of-the-week, weekend, turn-of-the-month and turn-of-the-year effects.

The holiday effect is defined as a seasonal anomaly that may exist in the daily returns on trading days before and/or after holidays. Non-holidays are defined as all trading days, excluding the pre-holidays and post-holidays. The holiday effect was identified as early as 1931 by Fields (Thaler, 1987: 170), but was not particularly well researched until the late 1960s. Research results have shown support for a holiday effect as an anomaly in its own right. The post-holiday mean returns are higher after weekends, when mean returns are usually lower. French (Thaler, 1987: 171) therefore concluded that the holiday effect is not merely a closed-market effect. Ariel (1990: 1621) concluded that the pre-holiday effect is not a manifestation of other calendar anomalies, such as a weekend effect or a January effect.

The search for seasonal anomalies in the international futures markets started in the early 1980s, with limited daily trading data available. The pre-holiday returns in the futures markets have shown higher mean returns than for other trading days, similar to the higher pre-holiday mean returns on the share markets. The close-to-close cumulative returns of pre-holidays contribute to a high proportion of the overall market return, much higher than the proportion of pre-holidays to non-holidays in the sampling periods.

The purpose of this study is to determine whether the holiday effect also exists in the South African futures market. The statistical significance of the holiday effect will be investigated for three South African futures contracts namely: All Gold Near Futures (ALGNF); All Industrial Near Futures (ALINF) and All Share Near Futures (AL-

SNF). The research results of the South African futures market holiday effect are compared with the holiday effects on the South African share market, as well as with the research findings on international share and futures markets.

The second section covers important contributions in the literature on seasonal anomalies in chronological order, focussing on the holiday effect. The third section covers the data description and method of analysis. The different holidays are discussed, as well as the handling of problem data. The empirical results are discussed in the fourth section and the research results are summarised in the fifth.

Review of related research

Share markets

Fields (Thaler, 1987: 170) was the first to study the weekend effect on the security markets. He investigated the conventional Wall Street wisdom at the time that

'the unwillingness of traders to carry their holdings over the uncertainties of a week-end leads to a liquidation of long accounts and a consequent decline of security prices on Saturday'.

He actually found that the Saturday prices tend to rise for the Dow Jones Industrial Average (DJIA). In a later study (1934) Fields also found a high proportion of positive returns on the trading days on the DJIA before long weekends (Thaler, 1987: 170).

The above average returns before holidays have been noted by various share market advisers. These advisers include Merrill who analysed the DJIA for the period 1897 to 1965, and Fosback who later (1976) studied the S&P 500 Index returns (Ariel, 1990: 1611). These two studies led the way to active research on the holiday effect.

Cross (Thaler, 1987: 171) studied the S&P 500 Index during 1973, and found that the mean return for Mondays was -0.18% and on Fridays 0.12%. French (Thaler, 1987: 171) following up on this research during 1980, obtained similar results. He found negative mean returns on Mondays, but with the other days showing positive mean returns. The highest returns were on Wednesdays and

Fridays. French (Thaler, 1987: 171) suggested that the negative mean return on Mondays could be attributed to some unknown 'closed-market effect'. If this were true, one can expect daily returns to be lower after weekends, as well as after holidays. However, the mean returns are higher than normal after holidays, excluding Tuesdays. Tuesdays show a negative mean return following a Monday holiday.

Detailed studies by Roll (Ariel, 1990: 1611) in 1983 found 'high returns accruing to small firms on the trading day prior to New Year's Day'. Studies by Lakonishok & Smidt (Ariel, 1990: 1611) in 1984 showed that daily closing prices also rise on trading days before Christmas. These studies highlight the importance of the holiday period at the turn of the year.

Rogalski (1984) analysed the effects of Mondays, weekends and holidays on the DJIA. The Friday to Monday close-to-close returns are on average positive for January, but on average negative for the rest of the year when holidays and holiday-weekends were excluded from the analysis. The mean returns were determined separately for the trading days after holidays and after weekends which include holidays. He reported that the mean returns on weekends which include holidays from Thursday close to Monday close are similar in sign and magnitude to returns from Friday close to Monday close. There is also no obvious relationship with firm size. The Friday to Tuesday holiday weekends differ from the above and are to a certain extent related to firm size. The two-day calendar holiday returns from Wednesday to Friday are greater for small firms. The mean return for Fridays, after Thursday holidays, is relatively larger in magnitude.

Lakonishok & Smidt (Thaler, 1987: 173) found that 51% of the capital gains of the past 90 years occurred on the pre-holidays, highlighting the size of the pre-holiday returns. Their research on the DJIA shows a mean return for pre-holidays of 0.219%, in contrast with the mean return of 0.0094% for other days. This gives a ratio of 23:1 for pre-holiday to other trading days returns.

Ariel (1990: 1614) researched the holiday effect on an equally weighted index of shares and a value weighted index of shares of the Centre for Research in Security Prices (CRSP) for the period 1963 to 1982. The pre-holiday mean returns are 0.528% and 0.364% for the indices respectively, compared to the non-holiday mean returns of 0.059% and 0.026% respectively. This pre-holiday to other day ratio of mean returns is 8.9 for the equally weighted index, while the ratio for the value weighted index is 14.0. The differences between the mean returns are statistically significant. The post-test period results from 1983 to 1986 also support the high mean returns for pre-holidays, and therefore supports the presence of a holiday effect. His research shows that pre-holidays represent only 3.19% of the 251 average trading days in a year, while 34.7% of the 20 year cumulative return has been earned on these pre-holidays. The pre-holidays with positive returns vary between 75% to 85.6% of total pre-holidays, as compared to the 53.8% to 55.8% of positive returns among the other trading days. These higher ratios of positive pre-holiday returns are significantly different from the rest of the trading days. Ariel (1990: 1614) found that the pre-holiday variance of returns is actually

lower than the variance of returns for all other trading days, and concludes that 'this fact serves to emphasise that the pre-holiday return is not a reward for bearing extra risk'. Ariel (1990: 1621) also concluded that 'pre-holiday returns are not a manifestation of other calendar anomalies', for example the January effect or the weekend effect. The high mean return on pre-New Year's Day is not driven by the strong January effect.

Pettengill & Jordan (1988) showed that pre-holiday returns are uniformly higher than on other trading days, regardless of the day of the week. Wednesdays have shown the highest pre-holiday mean return, with the lowest pre-holiday mean return on a Monday. The Monday pre-holiday mean return, however, is still four times higher than mean returns on other trading days.

Holidays and weekends are both considered a form of market closing. Lakonishok & Smidt (Fabozzi, Ma & Briley, 1994: 307) noted that the pre-holiday returns are two to five times higher than pre-weekend returns. They therefore suggest that another factor, other than the closed-market factor, is present. Coursey & Dyl (Thaler, 1987: 175) suggested that the weekend effect might be explained by psychological factors. It is also suggested that 'other behavioural explanations might incorporate variations in the mood of the market participants'. This will be more applicable to good moods before holidays and weekends and the bad moods on Mondays. These findings are supported by Deldin, Levin & Irwin (Fabozzi *et al.*, 1994: 308).

Pettengill (1989) has shown that the return on pre-holidays varies by holiday, day of the week on which the holiday falls, and firm size. He made use of the S&P 500 Index for the large firm portfolio. The mean return for post-holidays is less than the mean return for non-holidays of large firms, but not for small firms. The mean returns for days before and after holidays are significantly different from non-holidays, but only the mean returns for pre-holidays are significantly higher. The study has shown consistency of holiday returns over years.

A study by Kim & Park (1994) confirmed the high pre-holiday returns in the three major United States share markets and demonstrated that the holiday effect is also present in the United Kingdom and Japan share markets, even though the holidays and institutional arrangements differ from country to country. Various empirical studies provide evidence of international linkages of share market returns. Kim & Park (1994) used the Financial Times 30 Index (FT 30) of the UK, the Nikkei-Dow Index of Japan and the S&P 500 Index of the USA in their analysis. Their study has shown the holiday effect in the share markets of the different countries to be independent.

Kim & Park (1994) concluded that the Japanese holiday effect is not a closed-market effect. They further concluded that

'institutional factors such as trading methods, clearing mechanisms, settlement procedures, and bid-ask spreads cannot be possible explanations for international evidence of the holiday effect, because these institutional factors are different across countries'.

Futures markets

The trading in share index futures only began in 1982 (Khaksari & Bubnys, 1992: 534), therefore most studies in areas of futures price anomalies use small sample sizes. Research done in 1983 by Chiang & Tapley (Johnston, Kracaw & McConnell, 1991: 24) found a Monday effect and weekly seasonal effects in daily returns on a variety of futures contracts. The Dyl & Maberly research (Johnston *et al.*, 1991) of 1986 found that the S&P 500 Share Index futures shows a closed-market weekend effect.

Cornell (1985) found support for the findings of Rogalski (1984) regarding the S&P 500 Index, namely a Monday effect, but found no similar patterns for the S&P 500 Futures for the period May 1982 to July 1984. He concluded that the behaviour of futures prices is consistent with the efficient market hypothesis.

Johnston *et al.* (1991:25) studied the day-of-the-week effect in American GNMA, T-Bond, T-Note and T-Bill futures contracts. The negative Monday returns are associated with the weekend effect, as with share market returns, and not with holidays and other market closings. They found significant mean returns for Tuesdays after 1984, except for the T-Bill contracts. They excluded returns over holidays in the above-mentioned studies.

A study by Jordan & Jordan (1991) has shown significant turn-of-the-month and day-of-the-week effects, but no January or turn-of-the-year effects in the S&P 500 futures contract. Returns tend to be low on Mondays and high on Wednesdays and Fridays. Their results are not qualitatively different after omitting days following holidays.

A recent study (Fabozzi *et al.*, 1994) analysed holiday trading in futures markets for 16 different contracts. The mean pre-holiday return is 12 times higher than the non-holiday mean return for copper futures, and 170 times higher for Treasury Bill contracts. However, most of the pre-holiday mean returns do not significantly differ from the non-holiday mean returns. They further found six of the 16 futures contracts with higher post-holiday mean returns.

Fabozzi *et al.* (1994: 315) reported significantly lower trading volumes on the pre-holiday trading days for the 16 contracts investigated. Evidence exists that traders appear to avoid trading in periods prior to holidays. It is important to note that trading volume increases when the contract approaches its maturity date, making it more difficult to interpret holiday patterns. They also suggest that the lower volume and higher return pre-holiday trading are

'inconsistent with a theory of buying because of a positive holiday psychology. The evidence reported here is more consistent with the prediction of the inventory adjustment hypothesis'.

Fabozzi *et al.* (1994: 309) included weekday and weekend holidays in the sample to test for the calendar time hypothesis, which suggests that returns vary with the day of the week. The calendar time and trading time hypotheses are both rejected, because of too low pre-holiday returns during the mid-week and too high returns on Monday and Friday.

Chang, Jain & Locke (1995) analysed the volatility and price changes of the S&P 500 Index futures around the NYSE close. The volatility in the futures market drops sig-

nificantly when the NYSE closes, only to increase again at the close of the futures market. The futures market bid prices therefore follow a U-shaped pattern. They have found the Friday close in the futures market to be the period with the highest volatility, higher than the rest of the week. Their evidence suggests that 'the size of the market-closing effect on volatility increases with the anticipated length of time over which the market is closed' (Chang *et al.*, 1995: 61). They concluded that during the final minutes on the Friday, futures markets anticipate the weekend effect as found in equities.

South African research

Bhana (1985) studied the Monday effect on the JSE, and suggested that neither the calendar time nor the trading time hypothesis can explain the distribution of returns over the trading days of the week. The mean return had been negative for Mondays and positive for the rest of the other days. The highest return has been on Wednesdays. Bhana excluded returns for periods that included holidays. The difference in share returns on the different trading days indicates evidence of a market inefficiency. According to Davidson & Meyer (1993: 83) the Monday effect is no longer evident on the JSE.

The study of an equally weighted mining share index, industrial share index and an all share index showed an insignificant January effect (Bradfield, 1990). A significant July effect showed up in the mining shares, and a December effect was found in all three indices. Bradfield's (1990: 9) conclusive argument is 'that the significant seasonal effect in December is more likely to be a result of relatively less volatility than substantial return in December'.

Hattingh & Smit (1993) examined the seasonal patterns in the daily price movements of the Eskom 168, Post Office and RSA bonds, comparing them with the return patterns of the All Gold Index (AGI), All Industrial Index (AII) and All Share Index (ALSI) on the JSE. Their findings are in contrast to international research findings, namely that seasonal similarities exist between the bond and share markets. No holiday effects had been considered.

The seasonal patterns in the South African market were also investigated by Watson & Smit (1994: 155). The seasonal patterns of the AGI, the AII and the ALSI on the JSE were analysed and compared with the corresponding near futures contracts on the futures market. The results showed that seasonal similarities exist between the South African futures market and the spot market. The seasonal phenomena were analysed over different sampling periods, but remained stable. This research did not specifically consider any holiday effects. Watson & Smit (1994: 155) showed that the highest daily returns were from Tuesday to Thursday. The lowest daily returns were on Fridays and Mondays. All three indices show a significant day-of-the-week effect. Only the All Share Near Futures shows a significant turn-of-the-month effect.

Bhana (1994) evaluated the effect of public holidays on the returns of the companies listed on the JSE for the period 1975 to 1990. The pre-holiday mean returns were five times the mean returns accruing on trading days, excluding pre-holidays. The difference in the mean returns were

statistically significant. The data for the sampling period was sub-divided into two equal sub-sets, and no variation of the holiday effect was found over time. These results support research by Pettengill (1989), namely that there is no variation in the holiday effect over time.

The variances for pre-holidays are lower than for the other days, emphasising that the high pre-holiday return is no reward for extra risk (Bhana, 1994: 47). He further states that 'the holiday effect is intimately tied to the weekend effect'. Bhana's results support the closed-market hypothesis, where the days immediately before and after public holidays show a similar pattern to the weekend effect.

Nash (1994: 88) extended the study period of Bhana and included the AGI, the AII and the ALSI on the JSE. He demonstrated a consistently high return on all three indices on a Wednesday. This midweek effect has not been documented in international research. The daily returns were adjusted for the settlement period, after which the negative Monday effect disappeared. The AGI and ALSI displayed no significant day-of-the-week effect.

Summary

It is evident from research that a holiday effect exists in the international share markets and the futures markets. The holiday effect is also evident in the South African share market. The research methods used, however, were not uniform, making it difficult to directly compare research results.

Various sources indicate support for a weekend effect on the share markets, namely higher mean returns for a Friday

and lower mean returns for a Monday. Similar results have been found for the futures markets. It is also concluded that the days affected by Monday and Friday holidays cannot be seen in isolation from the weekend anomaly.

The existence of a holiday effect is supported by the following statistically significant results:

- The positive mean return for the pre-holidays is higher than the mean return for the non-holidays.
- There is a higher proportion of positive returns for pre-holidays than for non-holidays.
- The cumulative returns over the different sampling periods tend to be much higher for the pre-holidays than for the non-holidays, taking into account that pre-holidays are less than 4% of the total trading days on the market.

Researchers have found the difference in the mean returns for the different days of the week to be significant.

The theoretical views that may explain the holiday effect are summarised as follows:

- The holiday effect is due to the favourable holiday psychology on the last trading day before the holiday.
- It is consistent with the prediction of the inventory adjustment hypothesis.
- Volatility increases at market closing due to the extended period that the market will be closed.

Description of data and method

The raw data used in this research study was obtained from the Graduate School of Business of the University of Stellenbosch and from INET. Three futures data series were analysed, namely the ALGNF, the ALINF and the ALSNF. The raw data sample period runs from 5 January

Table 1 Official South African public holidays

Holiday	Date of holiday															
	1988		1989		1990		1991		1992		1993		1994		1995	
New Year's Day	1 Jan	Fri	1 Jan	Sun	1 Jan	Mon	1 Jan	Tue	1 Jan	Wed	1 Jan	Fri	1 Jan	Sat	1/2 Jan	Mon
Human Rights Day	-	-	-	-	-	-	-	-	-	-	-	-	-	-	21 Mar	-
Good Friday	1 Apr	Fri	24 Mar	Fri	13 Apr	Fri	29 Mar	Fri	17 Apr	Fri	9 Apr	Fri	1 Apr	Fri	14 Apr	-
Family Day	4 Apr	Mon	27 Mar	Mon	16 Apr	Mon	1 Apr	Mon	20 Apr	Mon	12 Apr	Mon	4 Apr	Mon	17 Apr	-
Founders' Day	6 Apr	Wed	6 Apr	Thu	6 Apr	Fri	6 Apr	Sat	6 Apr	Mon	6 Apr	Tue	6 Apr	Wed	-	-
Freedom Day	-	-	-	-	-	-	-	-	-	-	-	-	-	-	27 Apr	-
Workers' Day	6 May	Fri	1 May	Mon	1 May	Tue	1 May	Wed	1 May	Fri	1 May	Sat	1 May	Sun	1 May	-
Ascension Day	12 May	Thu	4 May	Thu	24 May	Thu	9 May	Thu	28 May	Thu	20 May	Thu	12 May	Thu	-	-
Republic Day	31 May	Tue	31 May	Wed	31 May	Thu	31 May	Fri	31 May	Sun	31 May	Mon	31 May	Tue	-	-
Youth Day	-	-	-	-	-	-	-	-	-	-	-	-	-	-	16 Jun	-
National Women's Day	-	-	-	-	-	-	-	-	-	-	-	-	-	-	9 Aug	-
Heritage Day	-	-	-	-	-	-	-	-	-	-	-	-	-	-	24 Sep	-
Kruger Day	10 Oct	Mon	10 Oct	Tue	10 Oct	Wed	10 Oct	Thu	10 Oct	Sat	10 Oct	Sun	10 Oct	Mon	-	-
Day of the Vow	16 Dec	Fri	16 Dec	Sat	16 Dec	Sun	16 Dec	Mon	16 Dec	Wed	16 Dec	Thu	16 Dec	Fri	-	-
Reconciliation Day	-	-	-	-	-	-	-	-	-	-	-	-	-	-	16 Dec	-
Christmas Day	25 Dec	Sun	25 Dec	Mon	25 Dec	Tue	25 Dec	Wed	25 Dec	Fri	25 Dec	Sat	25 Dec	Sun	25 Dec	-
Day of Goodwill	26 Dec	Mon	26 Dec	Tue	26 Dec	Wed	26 Dec	Thu	26 Dec	Sat	26 Dec	Sun	26 Dec	Mon	26 Dec	-
Voting Day	-	-	-	-	-	-	-	-	-	-	-	-	27 Apr	Wed	-	-
Voting Day	-	-	-	-	-	-	-	-	-	-	-	-	28 Apr	Thu	-	-
President Inauguration	-	-	-	-	-	-	-	-	-	-	-	-	10 May	Tue	-	-

1988 to 10 March 1995. The data consist of the daily closing prices of the near futures contracts.

The daily return is defined as the difference between the closing price on a particular trading day, and the closing price on the previous trading day, as a proportion of the closing price of the previous trading day.

The daily return is therefore modelled as:

$$R_t = (P_t - P_{t-1}) / P_{t-1}$$

with

R_t as the incremental return for day t ;

P_t as the closing price of the index on day t , and

P_{t-1} as the closing price of the index on the previous day, day $t-1$.

The pre-holiday return is defined as the incremental return, or difference, for the two trading days prior to the holiday. The post-holiday return is the difference between the trading day prior to the holiday and the trading day immediately after the holiday. The non-holiday return is the difference between two trading days, excluding the pre-holiday and post-holiday returns.

Eleven annual South African public holidays were involved in this study. See Table 1 for more details on the South African holidays. Seven of the eleven holidays occur during the first six months of the year. For purposes of future research note that the number of public holidays changed to twelve as from 1 January 1995. The new holidays are also included in Table 1. If any future holiday falls on a Sunday, the Monday will be a public holiday. A concentration of five holidays is now found in the period from 21 March to 1 May.

Both Good Friday and Ascension Day are holidays that cause a closing of the market. Other holidays may fall on weekends and will not affect the normal operation of the market. Weekend holidays are treated as follows:

- The Fridays and Mondays before and after weekend holidays are treated as pre-holidays and post-holidays. This is to ensure that no bias is built into the definition of the trading day prior to and following a public holiday.
- The alternative approach is to consider only public holidays that can provoke a closing of the market. This approach will only be used in a few comparisons.

It is necessary to deal with the day-of-the-week and other important seasonal effects when testing for the holiday effect. The holiday effect is estimated using the following equation which is derived from the model of Fabozzi *et al.* (1994: 319).

$$R_t = \alpha_1 + \beta_1 \cdot \text{TUE} + \beta_2 \cdot \text{WED} + \beta_3 \cdot \text{THU} + \beta_4 \cdot \text{FRI} + \beta_5 \cdot \text{JAN} + \beta_6 \cdot \text{PRE} + \beta_7 \cdot \text{POST} + \beta_8 \cdot \text{MD1} + e_t$$

with:

R_t as the excess return for contract at time t ;

α_1 as a constant that measures the mean return of Mondays;

β_1 to β_8 estimates of the coefficients of the dummy variables, measuring the incremental returns;

and the dummy variables as:

TUE to FRI All the non-Monday weekdays of the week (1 for daily return on the specific day and 0 for daily returns on the other days);

JAN All the trading days in January are included (1 for daily return in January and 0 for daily returns of other months);

PRE The pre-holiday is the last trading day prior to a holiday (1 for daily return on the pre-holiday and 0 for daily returns on the other days);

POST The post-holiday is the first trading day following a holiday (1 for daily return on the post-holiday and 0 for daily returns on the other days);

MD1 The turn-of-the-month, or month-end, includes the last trading day of the previous month and the first four trading days of the month. This is in line with Fosback (Ariel, 1987: 168) who found that stocks have a marked tendency to rise during the first four days of every month and on the last day of every month, also referred to as the month-end effect.

The multiple dummy variables separate the holiday effect from the day-of-the-week effects. The holiday effect estimators, namely β_6 for a pre-holiday and β_7 for a post-holiday, are therefore independent from the day-of-the-week effects. The regression model further tests whether the returns on Mondays are equal to the returns of the other weekdays. If the weekday returns are equal, the F -statistics for the first four dummy variables should be insignificant and the β estimates should all be close to zero.

Data for specific dates for all three near futures contracts are incomplete. The incomplete data, as listed in Table 2, is classified as follows:

- Data could not be found at Ivor Jones or SAFEX, and also no explanation for its absence. These few days are ignored and the previous available closing prices are used.
- Some of the missing data can be attributed to the closing of the market on the day before or after a holiday, for example on a Monday when the Tuesday is a holiday. These days are regarded as part of the closed-market holiday period.
- The market was closed after a weekend which includes a holiday, therefore this day is regarded as part of the closed-market holiday period.
- Holidays that fall on weekends do not necessitate extra closed-market days. There are ten such weekends with holidays in the sampling period. To test consistently for the holiday effect, the Friday is regarded as a pre-holiday and the Monday as a post-holiday.

The alternative is to regard the weekends with holidays as normal weekends. This aspect will also be tested, to ensure no significant changes take place.

Only the closing prices of the different futures contracts are available. As the opening values of the contracts are not available on the days following a closed-market period, it is not possible to determine whether any profit or loss is experienced in the non-trading period or during the active trading periods.

Table 2 Incomplete data and weekend holidays

Date	Missing data	Possible closed-market	New Year extra closing	Weekend holiday
	A	B	C	D
29-2-88	Mon			
5-4-88		Tue		
27-6-88	Mon			
2-1-89			Mon	
17-3-89	Fri			
5-5-89		Fri		
9-10-89		Mon		
6-12-89				Sat
6-9-90	Thu			
16-12-90				Sun
24-12-90		Mon		
31-12-90		Mon		
6-4-91				Sat
27-12-91		Fri		
31-5-92				Sun
10-10-92				Sat
1-5-93				Sat
10-10-93				Sun
25-12-93				Sat
26-12-93				Sun
1-1-94				Sat
1-5-94				Sun

Results

Analysis of holidays

A distribution of South African holidays, as per day-of-the-week, are listed in Table 3. Altogether 40% of the holidays in the research data are concentrated on Mondays and Fridays. The weekend holidays add another 18.8% of holidays. It therefore emphasises the importance of the days immediately before and after a weekend, as the possibility of a holiday effect may be strongly influenced by a weekend effect.

The holidays are not evenly distributed throughout the week. The number of pre-holidays and post-holidays differ from the actual number of holidays, due to the closing of the market for longer periods and where such a period includes more than one holiday. Four of the trading days are regarded as both pre-holiday and post-holiday, according to the definition of pre-holidays and post-holidays. The focus will actually be on the pre-holidays.

Four of the public holidays fall within the first half of the month, namely on New Year's Day, Founders Day, Workers Day and Kruger Day. Republic Day, Day of the Vow, Christmas Day and Day of Goodwill fall in the latter half of the month. These holidays may fall on weekends as well. The other holidays do not occur consistently in the same half of the month.

Post-holiday returns for Mondays and Tuesdays reflect holidays on Fridays to Mondays, which include weekends or longer periods of market closing. The post-holiday re-

Table 3 South African public holidays for the period 5 January 1988 to 10 March 1995

Day	Days of the week							Total
	Mon	Tue	Wed	Thu	Fri	Sat	Sun	
New Year's Day	2	1	1	-	1	1	1	7
Good Friday	-	-	-	-	7	-	-	7
Family Day	7	-	-	-	-	-	-	7
Founders' Day	1	1	2	1	1	1	-	7
Workers' Day	1	1	1	-	2	1	1	7
Ascension Day	-	-	-	7	-	-	-	7
Republic Day	1	2	1	1	1	-	1	7
Kruger Day	2	1	1	1	-	1	1	7
Day of the Vow	1	-	1	1	2	1	1	7
Christmas Day	1	1	1	-	1	1	2	7
Day of Goodwill	2	1	1	1	-	1	1	7
Voting Day	-	-	1	1	-	-	-	2
Presidential Inauguration	-	1	-	-	-	-	-	1
Total	17	9	10	13	16	7	8	80
Distribution of holidays	22.5%	11.3%	12.5%	16.3%	18.8%	8.8%	10.0%	-
Pre-holidays	5	8	11	15	25	-	-	64
Post-holidays	20	17	8	8	11	-	-	64

turns for Wednesdays to Fridays reflect mainly the one-day holidays, or one-day market closings. The kurtosis and skewness of the ALGNF, ALINF and the ALSNF are summarised in Table 4. The day-of-the-week analysis results are shown in Appendices A, B and C.

In general the ALGNF has a high pre-holiday kurtosis, also for a Wednesday, indicating a very steep distribution with long tails. The Wednesday pre-holiday returns are

Table 4 Kurtosis and skewness of near futures contracts

Near futures statistics	All days	Pre-holiday	Post-holiday	Non-holiday
ALGNF:				
Kurtosis	2.446	13.996	0.171	1.752
Standardised kurtosis	21.162	22.855	0.280	14.886
Skewness	0.312	2.509	0.458	0.197
Standardised skewness	5.400	8.192	1.495	3.348
ALINF:				
Kurtosis	11.220	2.449	1.874	11.277
Standardised kurtosis	97.085	3.999	3.060	95.828
Skewness	-0.971	0.950	-0.648	-1.001
Standardised skewness	-16.811	3.102	-2.115	-17.011
ALSNF:				
Kurtosis	3.903	3.949	1.368	3.867
Standardised kurtosis	33.775	6.449	2.234	32.859
Skewness	-0.380	1.573	-0.635	-0.428
Standardised skewness	-6.584	5.138	-2.075	-7.266

positively skewed. The rest of the days show similar flatter distributions. The ALGNF standardised kurtosis of 21.2 and standardised skewness of 5.4 indicate that the ALGNF daily returns differ significantly from a normal distribution. Both the pre-holiday and non-holiday returns differ significantly from a normal distribution. It is only the post-holiday returns of the ALGNF that do not differ significantly from a normal distribution.

The ALINF daily returns have a higher kurtosis for the non-holiday trading days. The ALINF standardised kurtosis of 97.1 and standardised skewness of -16.8 indicate that the ALINF daily returns differ significantly from a normal distribution. All of the ALINF pre-holiday, post-holiday and non-holiday returns differ significantly from a normal distribution.

It is only the Wednesday pre-holiday and post-holiday ALSNF returns that have a higher kurtosis than the non-holiday returns. The pre-holiday returns are all positively skewed, while the post-holiday returns are all negatively skewed, as are most of the non-holiday returns. The ALSNF standardised kurtosis of 33.8 and standardised skewness of -6.6 indicate that the ALSNF daily returns differ significantly from a normal distribution. All of the ALSNF pre-holiday, post-holiday and non-holiday returns differ significantly from a normal distribution.

From the results in Table 4 it is therefore concluded that all three sets of near futures prices differ significantly from a normal distribution. The t-tests and F-tests are only meaningful if the data are normally distributed. It is therefore concluded that the t-test and F-test results may not be meaningful. The Mann-Whitney test will be used to determine whether the difference in the mean returns between two variables is significant.

The ALGNF pre-holidays show positive mean returns for all weekdays, except for Fridays which have a slightly negative mean return. The ALGNF pre-holiday mean return of 0.47% is 40.2 times the mean return of non-holidays, which is 0.012%. Only the Monday post-holidays show a positive mean return, contrary to an expected negative Monday effect. The large negative post-holiday mean return for a Tuesday would, however, correspond with the negative return after a weekend market closing. The non-holiday weekdays have negative mean returns for Mondays and Tuesdays.

The ALGNF median is 0.25% for pre-holiday returns and -0.33% for post-holiday returns, while the median for the non-holiday returns is 0.00%. The difference in the medians is tested with the Mann-Whitney U-test. According to the H_0 hypothesis the median returns for the pre-holidays and post-holidays are equal to the median return for non-holidays. The H_0 hypothesis is not rejected at the 5% significance level, as indicated by the Mann-Whitney p-values of 0.17 and 0.44. The results are given in Table 5.

The ALINF pre-holidays show positive mean returns for Tuesdays, Wednesdays and Fridays. The ALINF pre-holiday mean return is 2.9 times the mean return for non-holidays. The Monday and Friday post-holidays show a positive mean return. The non-holiday weekdays have negative mean returns for Mondays and Fridays.

Table 5 Minimum, mean and maximum returns for the near futures contracts

Day		ALGNF	ALINF	ALSNF
Pre-holiday (PRE)	Minimum return	-4.89%	-1.72%	-1.61%
	Mean return	0.47%	0.24%	0.38%
	t-value	1.468	1.078	1.947
	Significance level	0.142	0.281	0.051
	Maximum return	15.78%	3.86%	4.91%
	Mean (WH excluded)	0.49%	0.18%	0.33%
	Median	0.25%	0.17%	0.17%
	Mann-Whitney -p	0.171	0.461	0.165
Post-holiday (POST)	Minimum return	-5.81%	-3.45%	-4.28%
	Mean return	-0.13%	0.11%	-0.01%
	t-value	-0.444	0.172	-0.461
	Significance level	0.657	0.863	0.644
	Maximum return	6.97%	2.73%	2.77%
	Mean (WH excluded)	-0.47%	0.07%	-0.12%
	Median	-0.33%	0.07%	-0.02%
	Mann-Whitney -p	0.439	0.687	0.711
Non-holiday (NONH)	Minimum return	-11.58%	-12.60%	-9.65%
	Mean return	0.01%	0.08%	0.06%
	Maximum return	11.20%	6.10%	5.22%
	Mean (WH excluded)	0.02%	0.09%	0.07%
	Median	0.00%	0.08%	0.06%
Mean return ratio:				
PRE/NONH ratio	WH included	40.25:1	2.92:1	6.18:1
PRE/NONH ratio	WH excluded	21.24:1	2.06:1	4.88:1
WH = Weekend holidays (weekends with a holiday on Saturday or Sunday)				

The ALINF median is 0.17% for pre-holiday returns and 0.07% for post-holiday returns, while the median for the non-holiday returns is 0.08%. The difference in the medians is tested with the Mann-Whitney U-test. The H_0 hypothesis is not rejected at the 5% significance level, as indicated by the Mann-Whitney p-values of 0.46 and 0.69.

The ALSNF shows positive mean returns for all pre-holiday weekdays. The pre-holiday mean return is 6.2 times the mean return for non-holidays. Monday and Friday post-holidays show a positive mean return. The non-holiday weekdays have negative mean returns for Mondays and Fridays.

The ALSNF median is 0.17% for pre-holiday returns and -0.02% for post-holiday returns, while the median for the non-holiday returns is 0.06%. The difference in the medians is tested with the Mann-Whitney U-test. The H_0 hypothesis is not rejected at the 5% significance level, as indicated by the Mann-Whitney p-values of 0.16 and 0.71.

The mean returns are positive for all three near futures on Tuesday and Wednesday pre-holidays and Monday post-holidays. The mean returns on post-holidays are negative for Tuesday to Thursday. The non-holidays show positive mean returns for Thursday and negative mean returns for Monday. Friday non-holidays do not show a high positive mean return, as supported by the literature study.

The minimum and maximum daily returns for the near futures are also presented in Table 5. The ALINF and the ALSNF show similar deviations for pre-holidays and post-holidays, where these deviations are also smaller than the deviations for non-holidays. It therefore shows that although returns are higher on certain pre-holidays and post-holidays, they are less volatile. The ALGNF pre-holiday shows the highest ratio of pre-holiday to non-holiday returns, but it also shows larger minimum and maximum value deviations than the other near futures contracts.

The mean returns for ALGNF change to 0.489% for pre-holidays, -0.303% for post-holidays and 0.023% for the non-holidays, where the ten weekends with holidays are regarded as normal weekends. The pre-holiday/non-holiday ratio changes to 21.24:1. The mean return for the non-holidays doubled, while the mean return for pre-holidays remained the same. The ALINF and the ALSNF non-holiday mean returns also show an increase, with a corresponding decrease in the mean return for the pre-holiday. The post-holiday mean returns are also smaller. The pre-holiday/non-holiday ratio changes to 2.06:1 and 4.88:1 respectively. The above results support the assumption of Fridays and Mondays of weekends with holidays, to be regarded as pre-holidays and post-holidays.

The ALGNF standard deviations vary between 2% and 5%. Wednesdays show the highest standard deviation for pre-holidays and is also associated with the highest mean return for the week. The higher Wednesday mean return may be attributed to the increased risk of higher gains or losses, as the higher standard deviation is an indication of the higher risk in mean returns for Wednesdays. The rest of the days show a smaller or similar standard deviation than the normal trading on non-holidays.

According to the H_0 hypothesis the standard deviations for the pre-holidays and post-holidays are equal to the standard deviation for non-holidays. The H_0 hypothesis is not rejected at the 5% significance level for the ALGNF, with the pre-holiday standard deviation regarded as equal to the standard deviation for non-holidays. The H_0 hypothesis is rejected at the 4.9% significance level for the ALGNF post-holiday standard deviation. The H_0 hypothesis is also not rejected for the day-of-the-week standard deviations, except for the pre-holiday standard deviation for Wednesday. See Table 6 and Appendix A for the ALGNF statistical test results.

The ALINF standard deviations vary between 0.7% and 1.5%. Most of the pre-holiday and post-holiday day-of-the-week standard deviations are smaller than the non-holiday standard deviations. This indicates that there is no extra benefit due to risk, as risk is evenly spread over the days of the week.

The equality of standard deviation H_0 hypothesis is not rejected at the 5% significance level for the ALINF, with the standard deviation for the post-holidays regarded as equal to the standard deviation for non-holidays. The H_0 hypothesis is rejected for the pre-holiday standard deviation at the 0.7% significance level. The H_0 hypothesis is also rejected for the pre-holiday standard deviations of Mondays and Thursdays at the 5% significance level. See Table 6 and Appendix B.

Table 6 Difference between pre-holiday, post-holiday and non-holiday variances

Comparison of variances	ALGNF	ALINF	ALSNF
Pre-holidays versus non-holidays:			
s_1^2/s_2^2	1.284	1.559	1.228
$F_{0.025}$ (at 5% significance level)	1.389	1.389	1.389
H_0 (accepted if variances are equal)	Accepted	Rejected	Accepted
Significance level	13.8%	0.7%	22.1%
Post-holidays versus non-holidays:			
s_1^2/s_2^2	1.391	1.237	1.069
$F_{0.025}$ (at 5% significance level)	1.389	1.389	1.389
H_0 (accepted if variances are equal)	Rejected	Accepted	Accepted
Significance level	4.9%	20.5%	66.8%

The ALSNF standard deviations vary between 0.9% and 1.9%. Most of the pre-holiday and post-holiday day-of-the-week standard deviations are smaller than the non-holiday standard deviation. This indicates that there is no extra benefit due to risk, as risk is evenly spread over the days of the week.

The H_0 hypothesis is accepted at the 5% and significance level for the ALSNF, with the standard deviations for the pre-holidays and post-holidays regarded as equal to the standard deviation for non-holidays. It is only the ALSNF post-holiday standard deviation of Wednesday that is significantly higher than the standard deviation for non-holidays on Wednesday. The H_0 hypothesis is rejected at the 2.4% significance level. The standard deviation of Tuesday pre-holidays are significantly higher than the standard deviation of Tuesday non-holidays, at the 1.5% significance level. The Thursday and Friday pre-holidays are significantly lower at the 2.7% and 0.9% significance level respectively. See Table 6 and Appendix C.

The day-of-the-week pre-holiday standard deviations are only significantly higher than the standard deviations of non-holidays for ALGNF on Wednesdays and for ALSNF on Tuesdays. The other day-of-the-week pre-holiday standard deviations for ALINF and ALSNF, which are significantly different, are significantly lower than the standard deviations of non-holidays. The mean returns are, however, not significantly different as shown in Table 5. It is therefore suggested that the higher pre-holiday mean returns are due to a few exceptionally high returns.

The frequency of daily gains and losses, or advances, for all three near futures are shown in Table 7. According to the H_0 hypothesis the pre-holidays and the post-holidays should have similar frequencies of positive returns as the non-holiday returns. The test results have led to the non-rejection of the H_0 hypothesis, namely that all proportions are equal for the pre-holidays, post-holidays and the non-holidays for all three near futures. Detailed results of the hypothesis tests are available in Appendices A, B and C for the different near futures.

The results of the regression analysis are tabulated in Table 8.

Table 7 Frequency of daily advances

Daily returns	ALGNF			ALINF			ALS NF			
	PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH	
Return = 0	Number	4	3	48	5	4	82	2	1	74
	% of total	6.3%	4.7%	2.9%	7.8%	6.3%	4.9%	3.1%	1.6%	4.4%
Return > 0	Number	36	31	846	41	38	966	39	32	934
	% of total	56.3%	48.4%	50.6%	64.1%	59.4%	57.7%	60.9%	50.0%	55.8%
Positive	Number	32	28	798	36	34	884	37	31	860
	% of total	50.0%	43.8%	47.7%	56.3%	53.1%	52.8%	57.8%	48.4%	51.4%
Negative	Number	28	33	827	23	26	707	25	32	739
	% of total	43.8%	51.6%	49.4%	35.9%	40.6%	42.3%	39.1%	50.0%	44.2%
Sample size		64	64	1673	64	64	1673	64	64	1673

Table 8 Regression analysis to test for the strenght of the holiday effect in the ALGNF, ALINF and ALSNF

Independent variable	ALGNF			ALINF			ALS NF		
	Coefficient	t-value	Sig. level	Coefficient	t-value	Sig. level	Coefficient	t-value	Sig. level
Constant	-0.000412	-0.2985	0.7653	-0.000342	-0.5265	0.5986	-0.000615	-0.8527	0.3938
Tuesday	-0.000331	-0.1785	0.8583	0.001689	1.9378	0.0526	0.000916	0.9461	0.3441
Wednesday	0.00106	0.5712	0.5679	0.001187	1.3602	0.1738	0.001036	1.0692	0.285
Thursday	0.002068	1.1097	0.2671	0.00195	2.226 #	0.026 #	0.002822	2.9009 #	0.0037 #
Friday	0.000655	0.3494	0.7268	-0.00016	-0.1812	0.8562	0.000126	0.129	0.8973
January	-0.0039	-1.9346	0.053	-0.001156	-1.2201	0.2224	-0.00174	-1.6531	0.0983
Pre-holiday	0.003859	1.2079	0.2271	0.001288	0.8574	0.3912	0.002696	1.6161	0.1061
Post-holiday	-0.00157	-0.494	0.6213	0.0000023	0.0015	0.9988	-0.001048	-0.6311	0.5279
Turn-of-the-month	0.001012	0.7306	0.465	0.001426	2.1911#	0.0284#	0.001691	2.3389 #	0.0193 #
R ²	0.004908	-	-	0.009641	-	-	0.012982	-	-
R ² (Adjusted)	0.000455	-	-	0.005210	-	-	0.008566	-	-
Durbin-Watson	2.01318	-	-	1.95354	-	-	1.99225	-	-
F-Ratio of model	1.1023	-	0.3584	2.17581	-	0.0267 #	2.93962	-	0.0029 #
Standard error of estimate	0.024761	-	-	0.011640	-	-	0.012928	-	-
MAE=	0.018353	-	-	0.007883	-	-	0.009217	-	-

Significant at 5% level

The regression model of the ALGNF shows that none of the variables are significant, although the month of January becomes significant at the 5.3% level. Both Thursday and the turn-of-the-month variables are significant in the ALINF regression model, with a significance level of 2.6% and 2.84% respectively. The ALSNF regression model indicates the Thursday variable to be significant at the 0.37% level and the turn-of-the-month variable at 1.93%. January is only significant at the 10% level. None of the regression models show that the pre-holiday or post-holiday variables are significant for any of the near futures contracts.

It does not make much difference to the model whether the ten weekends, with Friday pre-holidays and Monday post-holidays, are excluded or not.

The mean and median returns were determined for each of the three trading days before a holiday, the two trading days following a holiday, as well as the mean return for the non-holidays. See Table 9 for these results of the ALGNF, ALINF and the ALSNF. Results from Bhana's study (1994: 47) on the JSE shares are also included in Table 9.

The mean returns for all three near futures show an increase on the three days prior to a holiday, with the largest mean return on the pre-holiday. The post-holiday period is followed by lower or even negative mean returns. The ALINF and the ALSNF compare favourably with the normal trading on non-holidays. A post-holiday effect therefore does not appear to be present.

The ALGNF shows only positive mean returns for the two days prior to the holidays. These returns are much more positive than the non-holiday mean returns. The third day prior to the holiday and the two days following a holiday show large negative mean returns. It appears as if a negative post-holiday period may exist, but only for the ALGNF.

The ALINF shows positive returns for the days immediately before and after a public holiday. The third day before the holiday and the two days following the holiday compare well with the non-holiday mean return. The ALSNF shows only a small negative mean return on the trading day following the holiday.

Table 9 Mean returns on days prior to and days following holidays

Near futures		3 Days prior to holiday	2 Days prior to holiday	Pre-holiday	Post-holiday	2 Days after holiday	Non-holiday
ALGNF	Mean	-0.214%	0.073%	0.472%	-0.128%	-0.252%	0.012%
	Median	-0.110%	-0.208%	0.252%	-0.328%	0%	0%
	MW - p	0.449	0.75	0.171	0.639	0.704	-
ALINF	Mean	0.113%	0.192%	0.245%	0.110%	0.059%	0.084%
	Median	0.121%	0.105%	0.168%	0.073%	0.156%	0.081%
	MW - p	0.576	0.95	0.45	0.68	0.712	-
ALSNF	Mean	0.070%	0.236%	0.384%	-0.014%	0.032%	0.062%
	Median	0%	0.079%	0.167%	-0.017%	0.159%	0.058%
	MW - p	0.911	0.613	0.15	0.74	0.981	-
Bhana #	Mean	0.0698%	0.0732%	0.2620%	0.0395%	0.0571%	0.0547%

Bhana data source: Bhana, 1994: 47
MW - p = Mann-Whitney probability

The unpaired Mann-Whitney (MW) U-test is used to calculate the test statistic Z for the average ranks of the days before and after a holiday. The difference in median returns are not significant at the 5% level. The median returns of the second day before a holiday and the second day after a holiday are not significantly different from non-holiday media returns either. Therefore, these results do not support a significant holiday effect.

The cumulative returns for the ALGNF, ALINF and ALSNF for the period 5 January 1988 to 10 March 1995 are summarised in Table 10. A cumulative return is defined as the sum of the daily non-inflation adjusted returns over the total sampling period, in terms of the actual near futures contract values. The cumulative return of -189 for all the days of the ALGNF therefore reflects that the ALGNF contract dropped from 1769 on 5 January 1988 to 1580 on 10 March 1995.

The results are summarised as follows:

a. Positive cumulative returns for the pre-holidays are

found for all three near futures. The pre-holiday cumulative returns contributed to 17.6% of the total ALINF returns and 31.3% of the total ALSNF returns. The pre-holidays are only 3.6% of the total trading days, indicating that the total pre-holiday returns are not proportional to the number of trading days.

The cumulative return for the ALGNF is positive for the pre-holidays while it is negative for the non-holidays. This highlights the importance of the holiday effect in the ALGNF.

- Pre-holiday returns are higher than post-holiday returns.
- The ALINF and the ALSNF both show that the post-holiday cumulative returns are strongly influenced by the positive pre-holiday returns. Four of the trading days may be regarded as pre-holidays and post-holidays, with pre-holidays taking preference. The ALGNF however, shows that the same four days influenced the cumulative post-holiday returns more negatively.

Table 10 Cumulative returns on near futures contracts for the period 5 January 1988 to 10 March 1995

Contract	All days	Pre-holiday	Post-holiday	Non-holiday
ALGNF				
Cumulative return	-189	491	-69	-611
% of All day return	-	(+)	-	(-)
Post-holidays (including 4 pre-holidays)	-	-	-93	-
ALINF				
Cumulative return	5051	891	169	3991
% of All day return	-	17.64%	-	79.01%
Post-holidays (including 4 pre-holidays)	-	-	453	-
ALSNF				
Cumulative return	3418	1071	-53	2400
% of All day return	-	31.33%	-	70.22%
Post-holidays (including 4 pre-holidays)	-	-	272	-
Trading days	1797	64	64	1673
Proportion of total days	-	3.56%	-	93.10%

Table 11 Holidays and the turn-of-the-month (or month-end) effects

Near future	Statistical description	Pre-holiday + month-end	Post-holiday + month-end	Non-holiday + month-end	All days month-end
ALGNF	Mean return	0.321%	-0.400%	0.130%	0.113%
	Median	0.576%	-0.821%	0.077%	0%
	Mann-Whitney - p	0.585	0.083	-	-
	Standard deviation	1.905%	2.598%	2.219%	2.216%
ALINF	Mean return	0.184%	0.073%	0.219%	0.202%
	Median	0.195%	0%	0.177%	0.172%
	Mann-Whitney - p	0.764	0.395	-	-
	Standard deviation	0.880%	0.858%	1.120%	1.097%
ALSNF	Mean return	0.197%	-0.014%	0.232%	0.204%
	Median	0.140%	-0.037%	0.234%	0.167%
	Mann-Whitney - p	0.549	0.336	-	-
	Standard deviation	0.882%	1.256%	1.259%	1.234%
	Sample size	31	30	399	430

d. The post-holiday returns for the ALGNF are negative, as it is for non-holidays, and even for the sampling period over all.

The pre-holidays are 7.2% of the total turn-of-the-month trading days. The mean returns of the pre-holidays and post-holidays of all three near futures do not differ significantly from the turn-of-the-month non-holidays. The ALGNF standard deviations of the pre-holidays and post-holidays do not differ significantly from the turn-of-the-month non-holiday standard deviation. Only the ALSNF pre-holiday standard deviation and the ALINF post-holiday standard deviation differ significantly from the non-holiday standard deviation, at the 5% significance level. The statistics and test results are available in Appendix A to C, with some results summarised in Table 11.

The ALGNF pre-holiday turn-of-the-month mean return is higher than the mean return for the non-holidays, but not significantly so. The mean returns for the ALINF and ALSNF on pre-holidays are equal to the mean returns on the non-holidays. The standard deviations are actually smaller for all three near futures for the pre-holidays as compared to the non-holidays. It is therefore concluded that the pre-holidays do not contribute significantly to the turn-of-the-month effect. These two seasonal anomalies both exist in their own right.

Conclusions

The mean and median returns of the daily returns before and after a holiday were analysed, as well as the cumulative returns of the near futures contract indices. The pre-holidays showed higher mean and median returns for all three near futures contracts. None of these near future returns were significantly different from the mean and median returns for non-holidays. The cumulative returns for pre-holidays contributed much more to the overall cumulative return of the near futures than the proportion of pre-holidays of total trading days. The regression analysis of the near futures have not shown any significant pre-holiday or post-holiday effect in the South African futures market.

The holiday effect does not influence the significance of the turn-of-the-month effect. It is concluded that both these seasonal anomalies exist in their own right in the South African futures market.

It is finally concluded that the holiday effects are not large enough to be exploited on an ongoing basis in the South African futures market, to really benefit the active traders and investors. The pre-holiday returns are not sufficient reward for taking extra risk of trading on a specific pre-holiday. Investors who want to trade around the holidays anyway, may utilise the opportunities. The seller could benefit by the pre-holiday higher mean returns on specific days, while the buyer may benefit from trading on the post-holidays with lower prices.

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Appendix A All Gold Near Futures statistical analysis results

Statistic Description	All days						JAN	NON-JAN	PRE + MD1	POST + MD1	NONH + MD1	MD1
	3PRE	2PRE	PRE	POST	2POST	NONH						
Mean (average) return	-0.214%	0.073%	0.472%	-0.128%	-0.252%	0.012%	-0.345%	0.062%	0.321%	-0.400%	0.097%	0.113%
Pre-/Non-holiday ratio			40.2452									
Standard deviation	2.192%	2.540%	2.774%	2.888%	2.765%	2.449%	2.814%	2.437%	1.905%	2.588%	2.240%	2.216%
Sample size	64	64	64	64	64	1673	167	1630	31	30	399	430
Minimum return	-5.31%	-4.75%	-4.89%	-5.81%	-7.01%	-11.58%	-11.58%	-10.63%	-3.98%	-4.51%	-8.63%	-8.63%
Maximum return	5.56%	7.92%	15.78%	6.97%	5.42%	11.20%	6.14%	15.78%	4.27%	6.14%	6.29%	6.29%
Range	10.88%	12.67%	20.67%	12.78%	12.42%	22.78%	17.72%	26.42%	8.25%	10.65%	14.92%	14.92%
Average deviation	1.773%	1.932%	1.773%	2.212%	2.046%	1.825%	2.153%	1.806%	1.540%	2.009%	1.664%	1.656%
Kurtosis	-0.065	1.073	13.996	0.171	0.327	1.842	1.227	2.546	-0.121	0.075	1.445	1.409
Standardised kurtosis												
Skewness	0.161	0.824	2.509	0.458	-0.327	0.183	-0.614	0.472	-0.123	0.610	-0.262	-0.262
Standardised skewness												
Count=0	2	2	4	3	5	48	7	48	1	1	16	17
Count=>0	3.1%	3.1%	6.3%	4.7%	7.8%	2.9%	4.2%	2.9%	3.2%	3.3%	4.0%	4.0%
Count>0	32	30	36	31	35	846	82	829	17	11	214	231
Count<0	50.0%	46.9%	56.3%	48.4%	54.7%	50.6%	49.1%	50.9%	54.8%	36.7%	53.6%	53.7%
Count<0	30	28	32	28	30	798	75	781	16	10	198	214
Count<0	46.9%	43.8%	50.0%	43.8%	46.9%	47.7%	44.9%	47.9%	51.8%	33.3%	49.6%	49.8%
Summation	32	34	28	33	29	827	85	801	14	19	185	199
% of total days	50.0%	53.1%	43.8%	51.6%	45.3%	49.4%	50.9%	49.1%	45.2%	63.3%	46.4%	46.3%
% of cumulative return	-13.7%	4.7%	30.2%	-8.2%	-16.1%	19.6%						
Difference in proportion p>0			0.02	(0.04)			(0.03)		0.02	(0.16)		
p pooled			0.48	0.48			0.48		0.50	0.49		
β_{p1-p2}			0.09	0.10			0.06		0.13	0.17		
1.96 (s) = 5% level			0.18	0.19			0.12		0.26	0.33		
H0 accept (p1-p2=0)			Y	Y			Y		Y	Y		
Difference in variance			1.284	1.391					0.723	1.335		
s_1^2 / s_2^2			1.389	1.389					1.603	1.614		
$F_{0.025}$			1.284	1.391					1.383	1.335		
Ensure $s_1^2/s_2^2 > 1$			Y	N					Y	Y		
H0 accept ($s_1^2 = s_2^2$)			Y	N					Y	Y		
Significance level			13.8%	4.9%					18.0%	23.7%		

Statistic Description	Daily return	Monday			Tuesday			Wednesday			Thursday			Friday		
		PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH
Mean (average) return	0.024%	0.892%	1.181%	-0.148%	0.780%	-1.285%	-0.058%	1.086%	-0.209%	0.035%	0.624%	-0.726%	0.167%	-0.072%	-0.225%	0.058%
Pre-/Non-holiday ratio																
Standard deviation	2.477%	2.095%	3.178%	2.648%	2.521%	1.936%	2.217%	5.120%	3.444%	2.431%	1.913%	3.797%	2.605%	1.998%	1.716%	2.322%
Sample size	1797	5	20	325	8	17	340	11	8	347	15	8	338	25	11	323
Minimum return	-11.58%	-1.75%	-4.85%	-10.63%	-3.96%	-4.51%	-6.06%	-4.03%	-5.27%	-7.75%	-3.83%	-5.81%	-11.58%	-4.89%	-2.56%	-8.63%
Maximum return	15.78%	3.99%	6.78%	9.25%	4.27%	1.93%	10.54%	15.78%	6.14%	10.10%	3.25%	6.97%	11.20%	3.65%	3.50%	11.01%
Range	27.36%	5.74%	11.63%	19.88%	8.25%	6.44%	16.80%	19.82%	11.41%	17.85%	7.08%	12.78%	22.78%	8.54%	6.06%	19.64%
Average deviation	1.836%	1.423%	2.475%	1.990%	1.661%	1.530%	1.672%	2.822%	2.468%	1.818%	1.490%	2.520%	1.934%	1.495%	1.318%	1.710%
Kurtosis	2.446	1.148	-0.372	1.341	1.285	-0.795	1.425	8.485	0.894	1.582	0.867	2.183	2.423	0.475	0.977	2.078
Standardised kurtosis	21.162															
Skewness	0.312	0.482	-0.229	-0.100	-0.517	-0.109	0.355	2.732	0.573	0.280	-1.127	1.042	0.122	-0.091	0.852	0.416
Standardised skewness	5.400															
Count=0	55	1	1	7	1	1	11	0	1	10	1	0	10	1	0	10
Count=>0	3.1%	20.0%	5.0%	2.2%	12.5%	5.9%	3.2%	0.0%	12.5%	2.9%	6.7%	0.0%	3.0%	4.0%	0.0%	3.1%
Count>0	911	4	15	154	6	5	165	5	4	184	11	2	178	10	5	167
Count<0	50.7%	80.0%	75.0%	47.4%	75.0%	29.4%	48.5%	45.5%	50.0%	53.0%	73.3%	25.0%	52.1%	40.0%	45.5%	51.7%
Count<0	856	3	14	147	5	4	154	5	3	174	10	2	166	9	5	157
Summation	47.8%	60.0%	70.0%	45.2%	62.5%	23.5%	45.3%	45.5%	37.5%	50.1%	66.7%	25.0%	49.1%	36.0%	45.5%	48.6%
% of total days	886	1	5	171	2	12	175	6	4	163	4	6	162	15	6	156
% of cumulative return	49.3%	20.0%	25.0%	52.6%	25.0%	70.6%	51.5%	54.5%	50.0%	47.0%	26.7%	75.0%	47.9%	60.0%	54.5%	48.3%
Difference in proportion p>0		0.15	0.25		0.17	(0.22)		(0.05)	(0.13)		0.18	(0.24)		(0.13)	(0.03)	
p pooled		0.46	0.47		0.46	0.45		0.50	0.50		0.50	0.49		0.48	0.49	
β_{p1-p2}		0.35	0.14		0.25	0.29		0.25	0.36		0.17	0.50		0.18	0.25	
1.96 (s) = 5% level		0.69	0.28		0.49	0.57		0.50	0.70		0.34	0.98		0.35	0.50	
H0 accept (p1-p2=0)		Y	Y		Y	Y		Y	Y		Y	Y		Y	Y	
Difference in variance		0.626	1.440		1.293	0.762		4.438	2.008		0.539	2.125		0.741	0.546	
s_1^2 / s_2^2		2.607	1.772		2.326	1.843		2.066	2.325		1.905	2.325		1.685	2.069	
$F_{0.025}$		1.597	1.440		1.293	1.312		4.438	2.008		1.854	2.125		1.350	1.631	
Ensure $s_1^2/s_2^2 > 1$		Y	Y		Y	Y		N	Y		Y	Y		Y	Y	
H0 accept ($s_1^2 = s_2^2$)		Y	Y		Y	Y		N	Y		Y	Y		Y	Y	
Significance level		35.0%	21.2%		50.6%	37.4%		0.0%	10.7%		6.1%	8.1%		25.9%	10.9%	

Appendix B All Industrial Near Futures statistical analysis results

Statistic Description	All days						JAN	NON-JAN	PRE + MD1	POST + MD1	NONH + MD1	MD1
	3PRE	2PRE	PRE	POST	2POST	NONH						
Mean (average) return	0.113%	0.192%	0.245%	0.110%	0.059%	0.064%	-0.022%	0.069%	0.184%	0.073%	0.203%	0.201%
Pre-Non-holiday ratio			2.9193									
Standard deviation	1.063%	0.949%	0.944%	1.060%	0.951%	1.179%	1.399%	1.141%	0.878%	0.858%	1.102%	1.087%
Sample size	64	64	64	64	64	1673	167	1630	31	30	369	430
Minimum return	-2.57%	-1.93%	-1.72%	-3.45%	-2.80%	-12.60%	-3.76%	-12.60%	-1.72%	-2.26%	-5.24%	-5.24%
Maximum return	2.35%	3.86%	3.86%	2.73%	1.62%	6.10%	6.10%	5.49%	2.15%	2.15%	3.66%	3.66%
Range	4.92%	5.79%	5.58%	6.18%	4.42%	18.70%	9.86%	18.10%	3.87%	4.40%	8.90%	8.90%
Average deviation	0.808%	0.649%	0.685%	0.747%	0.699%	0.797%	0.989%	0.769%	0.629%	0.622%	0.769%	0.759%
Kurtosis	0.036	3.447	2.449	1.874	1.738	11.452	2.543	13.020	0.492	1.503	3.356	3.328
Standardised kurtosis												
Skewness	-0.415	1.243	0.950	-0.648	-1.128	-1.008	0.514	-1.228	0.268	-0.209	-0.368	-0.374
Standardised skewness												
Count=0	1	4	5	4	3	82	10	81	0	2	20	20
Count=>0	40	38	41	38	41	966	86	955	20	16	247	287
Count>0	62.5%	59.4%	64.1%	59.4%	64.1%	57.7%	51.5%	58.6%	64.5%	53.3%	61.9%	62.1%
Count<0	39	34	36	34	38	884	76	874	20	14	227	247
Count<0	60.9%	53.1%	56.3%	53.1%	59.4%	52.8%	45.5%	53.6%	64.5%	46.7%	56.9%	57.4%
Summation	24	26	23	26	23	707	81	675	11	14	152	163
% of total days	37.5%	40.6%	35.9%	40.6%	35.9%	42.3%	48.5%	41.4%	35.5%	46.7%	38.1%	37.9%
% of cumulative return	7.230%	12.295%	15.658%	7.016%	3.757%	140.21%						
Difference in proportion p>0			0.03	0.00			(0.06)		0.08	(0.10)		
p pooled			0.53	0.53			0.53		0.58	0.56		
β_{p1-p2}			0.09	0.09			0.06		0.12	0.14		
1.96 (s) = 5% level			0.17	0.17			0.12		0.23	0.28		
H0 accept (p1-p2=0)			Y	Y			Y		Y	Y		
Difference in variance												
s_1^2 / s_2^2			0.6414	0.8082					0.6346	0.6061		
$F_{0.025}$			1.389	1.389					1.603	1.614		
Ensure $s_1^2/s_2^2 > 1$			1.5591	1.2374					1.5758	1.6499		
H0 accept ($s_1^2 = s_2^2$)			N	Y					Y	N		
Significance level			0.7%	20.5%					5.9%	4.0%		

Statistic Description	Daily returns	Monday			Tuesday			Wednesday			Thursday			Friday		
		PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH
Mean (average) return	0.069%	-0.008%	0.388%	-0.034%	0.847%	0.001%	0.153%	0.251%	-0.167%	0.117%	-0.088%	-0.438%	0.218%	0.239%	0.388%	-0.047%
Pre-Non-holiday ratio																
Standard deviation	1.167%	0.903%	1.204%	1.538%	1.369%	0.784%	1.012%	0.946%	1.461%	1.003%	0.674%	0.983%	1.166%	0.890%	0.775%	1.089%
Sample size	1797	5	20	325	8	17	340	11	8	347	15	8	338	25	11	323
Minimum return	-12.60%	-1.21%	-2.26%	-12.60%	-0.69%	-1.36%	-3.65%	-0.89%	-3.45%	-3.26%	-1.72%	-2.50%	-4.81%	-1.35%	-1.07%	-7.07%
Maximum return	6.10%	1.13%	2.73%	4.95%	3.86%	1.46%	5.49%	1.70%	1.70%	3.19%	0.92%	0.73%	6.10%	2.15%	2.15%	3.63%
Range	18.70%	2.34%	4.99%	17.55%	4.55%	2.87%	9.15%	2.59%	5.15%	6.45%	2.64%	3.23%	10.91%	3.50%	3.21%	10.70%
Average deviation	0.79%	0.707%	0.940%	0.974%	0.971%	0.594%	0.721%	0.811%	0.864%	0.748%	0.481%	0.690%	0.819%	0.676%	0.505%	0.722%
Kurtosis	11.220	-0.656	0.472	15.264	3.193	-0.149	3.393	-1.540	4.590	0.889	1.588	2.579	3.809	0.115	3.040	7.282
Standardised kurtosis	97.085															
Skewness	-0.971	-0.214	-0.514	-1.983	1.580	0.194	-0.019	0.462	-1.692	-0.185	-1.174	-1.456	0.297	0.501	0.638	-0.888
Standardised skewness	-16.811															
Count=0	91	0	0	19	0	1	16	0	1	15	2	1	15	3	1	17
Count=>0	51%	0.0%	0.0%	5.8%	0.0%	5.9%	4.7%	0.0%	12.5%	4.3%	13.3%	12.5%	4.4%	12.0%	9.1%	5.3%
Count>0	1041	3	12	179	6	8	210	5	5	196	10	3	208	17	10	173
Count>0	57.9%	60.0%	60.0%	55.1%	75.0%	47.1%	61.8%	45.5%	62.5%	56.5%	66.7%	37.5%	61.5%	68.0%	90.9%	53.6%
Count<0	950	3	12	180	6	7	194	5	4	181	8	2	193	14	9	158
Count<0	52.9%	60.0%	60.0%	49.2%	75.0%	41.2%	57.1%	45.5%	50.0%	52.2%	53.3%	25.0%	57.1%	56.0%	81.8%	48.3%
Summation	758	2	8	148	2	9	130	6	3	151	5	5	130	8	1	150
% of total days	42.1%	40.0%	40.0%	44.9%	25.0%	52.9%	38.2%	54.5%	37.5%	43.5%	33.3%	62.5%	38.5%	32.0%	9.1%	46.4%
Difference in proportion p>0		0.11	0.11		0.18	(0.16)		(0.07)	(0.02)		(0.04)	(0.32)		0.08	0.34	
p pooled		0.49	0.50		0.58	0.57		0.52	0.52		0.57	0.57		0.49	0.50	
β_{p1-p2}		0.36	0.16		0.22	0.21		0.25	0.29		0.19	0.50		0.14	0.18	
1.96 (s) = 5% level		0.70	0.31		0.44	0.40		0.50	0.57		0.37	0.97		0.28	0.36	
H0 accept (p1-p2=0)		Y	Y		Y	Y		Y	Y		Y	Y		Y	Y	
Difference in variance																
s_1^2 / s_2^2		0.3451	0.6129		1.9047	0.8004		0.8895	2.1236		0.3335	0.7098		0.6593	0.4699	
$F_{0.025}$		2.807	1.772		2.326	1.843		2.088	2.325		1.905	2.325		1.685	2.089	
Ensure $s_1^2/s_2^2 > 1$		2.8976	1.6316		1.9047	1.8656		1.1242	2.1236		2.9968	1.4088		1.5166	2.0005	
H0 accept ($s_1^2 = s_2^2$)		N	Y		Y	Y		Y	Y		N	Y		Y	Y	
Significance level		4.4%	9.4%		13.6%	10.7%		68.6%	8.1%		0.0%	40.1%		11.9%	6.6%	

Appendix C All Share Near Futures statistical analysis results

Statistic Description	All days						JAN	NON-JAN	PRE + MD1	POST + MD1	NONH + MD1	MD1
	3PRE	2PRE	PRE	POST	2POST	NONH						
Mean (average) return	0.070%	0.236%	0.384%	-0.014%	0.032%	0.062%	-0.102%	0.085%	0.197%	-0.014%	0.204%	0.204%
Pre-/Non-holiday ratio			6.1787									
Standard deviation	1.191%	1.149%	1.174%	1.346%	1.237%	1.301%	1.309%	1.296%	0.882%	1.256%	1.258%	1.234%
Sample size	64	64	64	64	64	1673	167	1630	31	30	399	430
Minimum return	-3.10%	-2.01%	-1.61%	-4.28%	-3.10%	-9.65%	-3.66%	-9.65%	-1.07%	-3.68%	-4.98%	-4.98%
Maximum return	2.65%	4.91%	4.91%	2.77%	2.65%	5.22%	3.62%	5.22%	2.57%	2.36%	4.11%	4.11%
Range	5.74%	6.92%	6.52%	7.05%	5.74%	14.87%	7.28%	14.87%	3.65%	6.04%	9.09%	9.09%
Average deviation	0.876%	0.841%	0.824%	0.966%	0.965%	0.927%	1.006%	0.915%	0.630%	0.926%	0.918%	0.897%
Kurtosis	0.271	3.194	3.949	1.368	-0.141	3.957	0.519	4.304	1.330	1.500	1.846	1.922
Standardised kurtosis												
Skewness	-0.248	1.145	1.573	-0.635	-0.184	-0.420	0.002	-0.421	1.050	-0.688	-0.279	-0.248
Standardised skewness												
Count=0	8	4	2	1	2	74	9	68	0	1	16	16
Count=>0	12.5%	6.3%	3.1%	1.6%	3.1%	4.4%	5.4%	4.2%	0.0%	3.3%	4.0%	3.7%
Count>0	38	37	39	32	39	934	89	912	17	15	241	258
Count<0	59.4%	57.8%	60.9%	50.0%	60.9%	55.8%	53.3%	56.0%	54.8%	50.0%	60.4%	60.0%
Summation	30	33	37	31	37	860	80	844	17	14	225	242
% of total days	46.9%	51.6%	57.8%	48.4%	57.8%	51.4%	47.9%	51.8%	54.8%	46.7%	56.4%	56.3%
% of cumulative return	26	27	25	32	25	739	78	718	14	15	158	172
	40.8%	42.2%	39.1%	50.0%	39.1%	44.2%	46.7%	44.0%	45.2%	50.0%	39.6%	40.0%
Difference in proportion p>0			0.06	(0.03)			(0.04)		(0.02)	(0.10)		
p pooled			0.52	0.51			0.51		0.56	0.56		
χ^2_{1-2}			0.09	0.09			0.06		0.13	0.14		
1.96 (s) = 5% level			0.17	0.18			0.12		0.25	0.28		
H0 accept (p1-p2=0)			Y	Y			Y		Y	Y		
Difference in variance			0.8141	1.0693					0.4920	0.9975		
s_1^2 / s_2^2			1.389	1.389					1.603	1.614		
$F_{0.025}$			1.2283	1.0693					2.0327	1.0025		
Ensure $s_1^2/s_2^2 > 1$			Y	Y					N	Y		
H0 accept ($s_1^2 = s_2^2$)												
Significance level			22.1%	66.8%					0.3%	93.0%		

Statistic Description	Daily return	Monday			Tuesday			Wednesday			Thursday			Friday		
		PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH	PRE	POST	NONH
Mean (average) return	0.067%	0.275%	0.459%	-0.076%	0.718%	-0.262%	0.059%	0.588%	-0.119%	0.064%	0.375%	-0.853%	0.276%	0.214%	0.193%	-0.021%
Pre-/Non-holiday ratio																
Standard deviation	1.298%	1.222%	1.357%	1.594%	1.914%	0.899%	1.144%	1.553%	1.931%	1.192%	0.930%	1.631%	1.336%	0.838%	0.985%	1.179%
Sample size	1797	5	20	325	8	17	340	11	8	347	15	8	338	25	11	323
Minimum return	-9.65%	-0.89%	-2.18%	-9.65%	-1.20%	-2.01%	-5.70%	-1.36%	-4.28%	-3.85%	-1.07%	-3.68%	-6.03%	-1.61%	-1.12%	-4.98%
Maximum return	5.22%	2.35%	2.77%	5.22%	4.91%	1.29%	5.04%	4.27%	2.00%	3.41%	2.57%	0.99%	4.78%	2.36%	2.36%	4.84%
Range	14.87%	3.23%	4.95%	14.87%	6.11%	3.30%	10.74%	5.62%	6.29%	7.26%	3.65%	4.67%	10.81%	3.97%	3.48%	9.82%
Average deviation	0.923%	0.828%	1.127%	1.108%	1.321%	0.712%	0.810%	1.140%	1.203%	0.893%	0.670%	1.240%	0.964%	0.585%	0.699%	0.832%
Kurtosis	3.903	3.367	-0.758	5.365	3.499	-0.295	3.557	2.388	3.345	0.668	1.266	-0.098	2.197	1.760	1.277	2.554
Standardised kurtosis	33.775															
Skewness	-0.380	1.638	-0.228	-0.950	1.686	-0.242	-0.239	1.318	-1.468	-0.187	0.705	-1.023	-0.155	0.687	1.053	0.218
Standardised skewness	-6.584															
Count=0	77	0	0	14	0	0	16	0	1	15	1	0	12	1	0	17
Count=>0	4.3%	0.0%	0.0%	4.3%	0.0%	0.0%	4.7%	0.0%	12.5%	4.3%	6.7%	0.0%	3.6%	4.0%	0.0%	5.3%
Count>0	1001	2	12	171	5	7	199	5	4	190	11	3	206	16	6	168
Count<0	55.7%	40.0%	60.0%	52.6%	62.5%	41.2%	58.5%	45.5%	50.0%	54.8%	73.3%	37.5%	60.9%	64.0%	54.5%	52.0%
Summation	924	2	12	157	5	7	183	5	3	175	10	3	194	15	6	151
% of total days	51.4%	40.0%	60.0%	48.3%	62.5%	41.2%	53.8%	45.5%	37.5%	50.4%	66.7%	37.5%	57.4%	60.0%	54.5%	46.7%
% of cumulative return	796	3	8	154	3	10	141	6	4	157	4	5	132	9	5	155
	44.3%	60.0%	40.0%	47.4%	37.5%	58.8%	41.5%	54.5%	50.0%	45.2%	26.7%	62.5%	39.1%	36.0%	45.5%	48.0%
Difference in proportion p>0		(0.08)	0.12		0.09	(0.13)		(0.05)	(0.13)		0.09	(0.20)		0.13	0.08	
p pooled		0.48	0.49		0.54	0.53		0.50	0.50		0.58	0.57		0.48	0.47	
χ^2_{1-2}		0.50	0.16		0.25	0.21		0.25	0.36		0.17	0.35		0.14	0.23	
1.96 (s) = 5% level		0.98	0.31		0.49	0.41		0.50	0.70		0.33	0.69		0.27	0.44	
H0 accept (p1-p2=0)		Y	Y		Y	Y		Y	Y		Y	Y		Y	Y	
Difference in variance		0.5877	0.7246		2.8019	0.6186		1.6985	2.6270		0.4849	1.4896		0.5050	0.6979	
s_1^2 / s_2^2		2.607	1.772		2.326	1.843		2.086	2.325		1.905	2.325		1.685	2.089	
$F_{0.025}$		1.7015	1.3800		2.8019	1.6166		1.6985	2.6270		2.0622	1.4896		1.9802	1.4329	
Ensure $s_1^2/s_2^2 > 1$		Y	Y		N	Y		Y	N		N	Y		N	Y	
H0 accept ($s_1^2 = s_2^2$)																
Significance level		29.9%	26.8%		1.5%	13.7%		15.9%	2.4%		2.7%	34.0%		0.9%	32.9%	